

Figure 2.1 The values from Example 2.1 plotted on a number line; typical for floating- point number systems, they are unevenly spaced between the minimum (0.5) and the maximum (3.5).

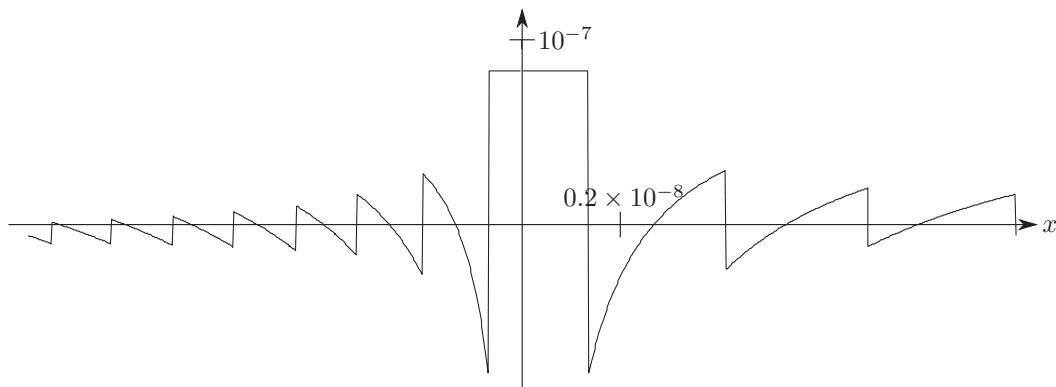


Figure 2.2 Values of $f(x)$ from Example 2.5, computed using IEEE floating-point arithmetic.

```

function SIMPLE-SUM( $\vec{x}$ )
     $s \leftarrow 0$                                  $\triangleright$  Current total
    for  $i \leftarrow 1, 2, \dots, n$  :  $s \leftarrow s + x_i$ 
    return  $s$ 

```

(a)

```

function KAHAN-SUM( $\vec{x}$ )
     $s, c \leftarrow 0$                              $\triangleright$  Current total and compensation
    for  $i \leftarrow 1, 2, \dots, n$ 
         $v \leftarrow x_i + c$                      $\triangleright$  Try to add  $x_i$  and compensation  $c$  to the sum
         $s_{\text{next}} \leftarrow s + v$              $\triangleright$  Compute the summation result of this iteration

         $c \leftarrow v - (s_{\text{next}} - s)$   $\triangleright$  Compute compensation using the Kahan error estimate
         $s \leftarrow s_{\text{next}}$                      $\triangleright$  Update sum
    return  $s$ 

```

(b)

Figure 2.3 (a) A simplistic method for summing the elements of a vector \vec{x} ; (b) the Kahan summation algorithm.

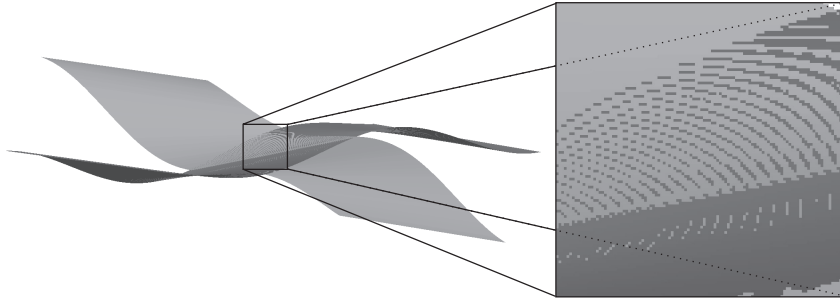


Figure 2.4 z-fighting, for Exercise 2.6; the overlap region is zoomed on the right.